

# THE FANTOPOLOGIST

Whole Mumper 3.

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The universe is wider than our views of it. Yet we should oftener look over the tafferel of our craft, like curious passengers, and not make the voyage like stupid sailors picking caku. Be a Columbus to whole new worlds within you, opening new channels, not of trade, but of thought. -- Henry David Thoreau

#### EDITORIAL

Charles Lamb, in his delightful essay on "The Origin of Roast Pig", has admirably characterized the role of the amateur in the development of civilization, a role replate with ludicrous errors, yet studded with occasional pearls of novelty. Such pearls, to continue the metaphor, are truly cast before swine, for the amateur very often lacks the background ad power to develop the ideas which he has come by as the result of a fortuitous combination of events. This fact contributes in no small degree to the apathy and reticence of the novice, who is loath to disclose his discoveries to the derision of those informed individuals who may recognize his efforts either as heinous fallacies or as unconscious duplications of antecedent systematic developments. He may, in short, find himself in an embarrassing condition of dishabile, running Archimedes-like down the street screaming "Eureka," when the information may be no more novel than a cake of floating soap.

It is for this reason that we have found it necessary to fathom the very depths of our courage in launching what may be but an unworthy raft upon uncharted seas, with neither rudder nor compass, nor yet any knowledge more positive than that the sea is salt. Our apprehensions have been overcome only by the realization that this same sea washes the most distant shores, and may conceivably leave some bit of driftwood to light with myriad hues the fire to which it may eventually find its way.

The Fantopologist, therefore, abominable craft that it is, will refuse neither a cargo of guano, nor of jewels for the Sultan of Baghdad. It will have no traffic with exclusion, for it recognizes the values of both science and philosophy, logic and mysticism, and of the known and the unknown. Kurt Lewin conceived of reality as a dimension, a continuum rather than a terminus, and it is in keeping with this spirit that the contents of the magazine will range all the way from tongue-in-cheek to cheek-by-jown. We shall seek for those ideas which are "topologically different" from those commonly received, without being yet quite "fantastic" -- the "fantopologically different", if you please. The most illustrious hope that may be entertained in behalf of this venture is that it may serve as a detonator to the explosive train of thought, and may leave some slight trace upon the seismograph of truth.

Zer-Kan, and he scoffs at wisdom and foolishness alike. He is the skipper of the craft.

.- H. T. McAdams -- W. I. Case

THE BIG BIRD

By

Bill Case

"I see, " murmured Dr. Beutter, who, like many of his kind, may actually have seen much or little.

Little Danny Bartell Squirmed in the huge leather chair which almost engulfed him. Danny was embarrassed and unhappy. Danny's

parents were unhappy although not a whit embarrameed.
"I see," said Dr. Beutter again, making a reflective arch of his two deligate hands on the chiny desk top. "How, Mr. Bartell, would you eay that this, ab - impression of Danny's is of long

"No, no," said Mr. Bartell. "It's just recently that Danny started talking about this bird. Couldn't have been more than two weeks ago, He is so intent, his description so vivid. It's as if

he is absolutely convinced that he sees this huge creature out there.".
"Um," said Beutter, "Well, of surse, these things are not at all unusual in children of Danny's age and temperament. Admittedly he is very consistent in his descriptions, but, again --

"What are we to do?" interrupted Mrs. Bartell plaintively.

"We can't let him continue this way. It's unhealthy."

"Unhealthy perhaps, Mrs Bartell yet not as unhealthy as you fear. This imaginative tendence is a sign of intelligence. It's just that we must distract Damies alers wind and direct his thoughts into more reasonable charmers."

Danny spoke up heatedly: "Aw you don't know anything.

better watch cut, too."

Boutter leaned forward, quissically intent. "Why. Danny?"

he murmured.

"'Cause They don't like people the laugh at them. That's why they're sending this bird. Be's gonne grab up the whole world and fly off with it. But he won't huse me.

"Mo?" queried Beutter "why not Danny?"

"Cause I can SEE the bird and YOU can't. 'Cause I do what

They tell me."

"They Danny? Who are these people you keep talking about?" They re NOT people, they re -- well. I denno -- I never saw But I know what they want, cause they send me messages." "Ah, " said Dr. Beutter.

"Sure. Sometimes I'll be lockin in my comic book, and when I turn the page there'll be a message there instead of comics. Or when I dig up dirt I sometimes find a rock with a message scratched on 11 "

"Shades of Charles Fort!" chucked Ben ser, leaning back confortably.

Danny just fromed and closed his lips firmly as a signal that he would volunteer nothing more. Mr. Bartell looked pained. Mrs. Bartell looked distraught. Beutter leaned forward again and concisely pictured what Danny had repeated to them time and again:

toward Earth from the general Sirection of Jupiter, and is now somewhere outside the moon's orbit. This bird, at the bidding of certain beings, is intent upon grasping Earth in its talons and flying away to where "They" reside. Seemingly "They" intend to renovate the

planet after which they will turn it over to the bird to plant in the skies again. Believers, like Danny here, will not be harmed but will stay with the planet and take part in its new existence."

Bevtter paused while everyone looked glum. He said brightly "I do not believe the astronomers have noticed anything unusual in the skies. Odd, odd. Can you see the bird from this window, Danny?".

"No," said Danny flatly.

"At what times of the day or night do you see it?"

"Any ol' time I want to except when people that don't believe are around."

"Naturally," said Beutter. "Well --"

Here followed Beutter's reassuring instructions to Danny's parents -- instructions calculated to ease the concern of the parents more than to actually divert the boy from his visions. After many sighs and shaking of heads, the Bartells were ushered out of the impressive sanctum of Dr. Beutter. The door closed silently in benediction.

Beutter returned to his desk and sank wearily into the soft chair. He did not yet press the buzzer that set in motion the procedure by which anothe, harried client would be ushered in. He thought: This stupid posturing and posing for the benefit of an ignorant mass of nerves called humanity. Doctor Beutter: As if in this pitiful title there reposed authority, genius, infallibility. And what did he give in return? Nothing: babblings, solumn airs, unctous manners. He smiled sadly, reflecting that you couldn't tell them the truth about themselves. You just couldn't.

He pressed the buzzer.

The door opened. Miss Halloran herded a nervous dowager into the room. Beutter looked at her keenly. Her jittery glance flickered about the room, taking in the expensive paintings, the softsilent rug, the huge impressive window which looked out upon the great city. Her gaze finally rested on Beutter. She started to speak, but her mouth dropped ajar like the scoop on a power shovel as she realized that the eminent Dr. Beutter was laughing silently, almost hysterically, and was paying her no attention at all, none at all.

Beutter was convulsed, and his laughter was indeed semihysterical, for it was obvious that the nervous dowager had seen nothing through the window, and Beutter could only imagine the state of her nerves if she could REALLY see what was out there, this side of the moon now, big as the sky, relentless and imperturbable -soon to grasp Earth between its incredibly enormous talons.

#### THE END

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## Excerpt from "THE BOOK OF ZAR-KAN"

Of earth and fire are you. Coarse earth calls forth heaven's jagged fire, and in this fury is creation and destruction. Here dwells the Self, borne upward on the flames, pressed into ignominious mud. But the storm is HERE, and not without: Ask not who sends it, for YOU must answer!

### PARTING THEY ONLY SAID THE PSAIM WAS DEAR

Should I be analysed only because the window is an obsession

I saw a window when I was born my mother saw one in the third month I was in her womb let this stump these feeble neurologists I refuse to count the malady singular

I was born

in an age Subsequently to be known as the are of windows

I will burn behind a window and be buried beneath a wintow how silly to may the eye is a window

and then

there is my art what window ever obscured more than this

Indeed, in this age of windows what indeed ever obscured more than this

-- J. C. Crews

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#### THE UNIVERSAL HEART

It comes upon a quiet, starry night, From depths of solemn wonder. Deep felt, all-encompassing. It bests like distant thunder. Ah, where, where to seek? What depths of feeling plumb: What search initiate, what probings Make for silent foxfire, hidden, dumb? Beat! Beat! You hear it? Tis the blood of Being, Rushing eternally, hear it? Beyond touch, beyond seeing -But 'tis there, doubt not; Though all Isve ever known, The only heart I've ever REALLY heard, Is here and now - my own.

## From THE BOOK OF ZAR-KAR

#### THE NORTHERN MEN

By special permission W. L. Casa

At last Pantogar came unto Zar-Kan's house, perched like a gray eagle upon the jutting, wind-swept hill. The journey had been long, the climb strenous, the thin, chill air burdensome; but now the house of Zar-Ken was reached, and Pantogar rested briefly before saying to

the white-haired prophet:

"Zar-Kan, I have heard from some that you are a wise man. I seek your counsel. My people have come upon strange ways, and I know not what to make of it. Though I am chieftain, and though the letter of my commands is obeyed; yet I am awars of an emptiness of spirit. The temples of worship are never smpty, yet the people are insincere, I fear. The nights are filled with the sounds of unbridled revelry and naught that I or my guards can do will forestall it for long.

Zar-Kan said: "You seek to know, Pantogar, how you may once

more direct your paople into the accustomed and moral ways?"
"Yes, Zar-Kan. What is this evil? Never has our community bean more prosperous, never has there been more cause for contentment and thanks-giving. But though the gods should be adored and praised for their many kindnesses, there is never a worthy sign of either gratitude or contentment."

"This discontent grows?"

"Yes, in spite of all. It is almost as if the people resent the

prosperity and peace that is theirs."

Zar-Kan gazed steadfastly at the blue and gray streaked skies. that made frigid patterns beyond the frame of a high window cut into the stone of his house. Long he gazed, and Pantogar finally spoke: "What would you tell me, Zar-Kan? I have gold to reward you if

you will but guide me truly."

Then Zar-Kan said: "They are from the north, eternally from the north, and none shall stand before them. They come from the northern hills and from the northern skies and from that within which is ever cold and clear and eager. They shall come and neither your guards nor priests nor gods shall prevail against them, for they are barbarland and fear not. Their coming is a Siva-coming, a killing and a giving of life. There shall be a mighty fear, a mighty conflict and a mighty destruction, and from the chaos shall rise the epiphenomenon we call civilization. For so it has ever been and will be."

Pantogar said: "Zar-Kan, what is this foolishness you speak?

What of the troubles I have related? What of my people?"

Zar-Kan said: "It is falsely written that heat is life and cold is death: I say contrarily. The cold is in their hearts and minds and blood. They turn always toward the warmth, the comfort, the ease, but their essence is of the north and that which is in them compells them to cast saids the warmth and comfort and ease wherever found, however desired, for so it is written. And there is a great sadness on them

and a yearning. There is something of hate in them, too, for so it must be if they seek always destruction; but there is compassion in them too, for so it must be if their coming is to be a siva-coming. Pantogar, they hate your laws and your gods and your customs. They will crush your idols and raze your temples and make a mockery of your moral creed. It is their destiny to conquer, and when they have encompassed your world and mine they will scream a challenge at the sun and stars and defy the spirits of hearth and hell to daunt them. For they are masters and leaders and seekers, and the primal urge to conquer burns like a white, cold fire in their breasts. They are beautiful and terrible and lonely, for they may never stop for the careas, the sip of wine; they are a coming and a going, and they may never pause."

Pantogar was deeply troubled. He said: "What is it you seek to tell me, Zar-Kan? Who are these unholy creatures? From whence come they?"

And Zar-Yam Said: "They come from every spirit that chafes, from every soul that aspires. In their most cherished possession they see a yoke, in every law a barrier, in every creed a shackle, for within-them is the cold fire that would leap and soar; and every temple stands upon a foundation of quicksand. Though time turn full cycle a trillion times, they all not die, nor their fury diminish. You, Pantogar, are a chieftain because your people rose from barbarism and hunger and fear, and made themselves laws to preserve that which they had gained. You are the symbol of those laws. But the wheel continues to turn, and you will go down and your people will go down. In their ignorance and fear they will hate that which they should love, and love that which they should hate."

Pantogar arose fearfully. "Zar-Kan," he said, "surely you know

not what you say, for the meaning of your words is madness."

Zar-Kan said: "The meaning of all words is madness."

Pantoger said: "I depart Zar-Kan, and a curse upon you and your foolishness. Much time and effort have I wasted in order to speak with you, and you jest or speak from a disordered mind. Instead of truth you give me fictions. Instead of fact, you give me idle words."

a god a countenance, it will blind you. We must ever peer above below, alongside, but never upon it, for if there be madness, that

Pantogar left Zar-Kan's house in great anger and returned no more.

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CLEARLY, SOCRATES;

What is the best that a person can do?
What is the most he can give?
What is his dominant purpose in life?
What is his reason to live?

-- H. T. Mcadams

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## H. T. MoAdams

when, in the course of human events, it becomes necessary to use the word "is", we have sinned the too great sin. Because every statement employing this monosyllable is either a redundancy or a lie. Of course, the disconcerting thing about all tris is the fact that any statement at all implies a usage of this verb.

Wathematics, according to L. Wittgenstein, is only a "vast tautology", and the most that it ever manages to say is that "a is a " The apparent variety of mathematical systems is only an unfolding of the numerous symbolic means of accomplishing this end. According to E. T. Bell, better known to science fiction fans as John Taine, this thesis of wittgenstein's was directly responsible for Carnap's development of the logical syntax of language.

As an example of such tautology, let us consider the well-known maxim: Genius is madness. If indeed the two concepts are identical, then we would require only one term for the two ideas, and would not even need it, since the fact would be obvious at the outset. By finding it necessary or appropriate to make such a definition, we have implied a certain lack of identity between the two equated concepts, and this subtle difference is the only condition which invests the statement with any meaning. Negative statements do not come off any better in the general scheme of things, for to say that a thing is not so-and-so is virtually to imply that it is so-and-so, at least in some respects. The negated statement implies a near-sameness absolutely essential to communication.

In other words, it makes little difference whether we use "is" or "is not", so long as our inferences are in order. It is only by inference that communication is possible, because if two concepts actually are identical, then we have actually said nothing. Ferhaps that is why all theories eventually lead to anomaly. With all the inferences and counter-inferences built around "is" and "is not", a balance is very unlikely.

The indicative mode in language, therefore, is actually a subjunctive mode, and "reality" is only a quasi-reality. Charles Fort found it amusing to poke fun at the seriousness with which "science" regards these precious tautologies, and conceived of "reality" as a continuum, and as a unity, about which we have found out nothing, "because there is nothing to be found out." "Existence" is only a quasi-existence, concected out of the attempt to "be" something, by excluding something else. Fort was anticipated, perhaps, by Hans Vaihinger, who, in his "Philosophy of the As If" attempted to reduce all reality to a set of fictions.

Of course Vaihinger may have been anticipated by Heracleitus when he said that we can not step twice in the same river. But then we can not step in the SAME river even ONCE, because then it as not a river at all: it is a bath-tub.

# UNCERTAINTY: THE COME OF A NEW PHILOSOPHY

By

#### Wm. I. Case

The student of physics is familiar with the famous Heisenberg Principle of Uncertainty. It is my wish to point out some further implications of this principle, implications which lead inevitably into general philosophic considerations. Particularly, these implications point to a new type of philosophy called cruxism.

The Heisenberg principle may be illustrated in an imaginary experiment in which a physicist attempts to observe the position and velocity of an electron by using a hypothetical super-microscope. In determining its position the velocity of the electron is altered; likewise, when its velocity is determined, its position is altered. Thus it is seen that discovering the fundamental nature of the electron runs into formidable, if not impassable, barriers. The effect of this impasse on the quest for the ultimate secrets of life and matter are obvious.

A generalized uncertainty principle can be applied to psychology and philosophy as well. The psychologist, attempting to determine precisely what motivates certain human actions, is driven by analysis from one stopping-off place backward to the next, and so on, until he is forced to consider matters like electro-neural impulses, brain waves, and other physio-psychical manifestations which are themselves incapable of further analysis, or are based upon unanalyzable substances. In philosophy the question of mind is of the utmost importance. We may ask ourselves, "What is mind?", but in examining the cuestion we find ourselves in the anomalous position of being the observer AND the observed, and completely at a loss to know where the one or the other has jurisdiction or whether either actually exists independent of the other.

In pursuing these thoughts to the utmost, it is likely that the seeker of knowledge will find himself involved in philosophic matters of the profoundest type. Ultimately the seeker must arrive, as I believe at any rate, at a sense of ABSOLUTE UNCERTAINTY. Every quest of whatever type must inevitably shatter on the rocks of paradox and uncertainty. It is this very paradox, this very uncertainty, which we must accept if we are to evolve an adequate science and adequate philosophy.

Picture this situation: a researcher is examining an unclassified object for the purpose of determining its exact nature. He finds -- invariably -- that the nature of the object in toto eludes him because of the effect of his instruments or of the act of observing; yet to eliminate the instruments or the observing act is to eliminate one face of that object's actual nature. The observer rightly concludes that 'he ultimate nature of the object is therefore uncertain; he cannot logically conclude otherwise.

Now here we introduce another factor, this: if the nature of the object is uncertain, then the EXISTENCE of the object is uncertain. That is, the observer, knowing the object only in aspect, cannot be sure that the TOTAL, or ultimate nature of the object is not entirely foreign to the observer's limited conception of it. When we look at a star in the night skies, are we actually seeing that star in existence, or any star at all? Perhaps not: that star may have exploded and vanished years before we were born; we see merely the light which commenced its journey before the cataclysm. Or perhaps it isn't a star at all; perhaps a gaseous nebula, actually attentuated and misty if viewed at a closer vantage point. Furthermore, if we were to view the nebula from within, we might be quite unaware that it existed, so dispersed would it be. In other words, we put labels on things depending upon the perspective, location, and relation of ourselves to those things. What they actually are - if they exist - we simply cannot say for sure.

The observer, as we have already seen, finds himself to be a quantity as unknown as any object under study, and for the same reason. We have this situation then: not only is the nature of the object uncertain; its very existence is uncertain, and, furthermore, the existence of the observer is uncertain. We have arrived then at a broader principle than Heisenberg's -- a principle which says: EVERYTHING is uncertain.

While this brief exploration of certain obvious considerations can in no way qualify as thorough justification for the cruxist principle of absolute uncertainty, it is hoped that some few who read this will be tempted to further examination of this principle.

# SPACE OF 31 DIMENSIONS

By H. T. McAdama

I know. I should beat a hasty retreat to the nearest booby-hatch and give myself up. But I have it on good authority that it is possible to construct spaces of 2/3 dimensions, 0.4123 dimensions, or even pi dimensions.

In other words, the number of dimensions in a given space does not have to be integral.

Has it ever occurred to you that the inconsistencies attendant in any physical theory, based on three, four, or any other number of dimensions might be the result of quantization. Maybe our apparent space-time continuum has only 3.999999 dimensions instead of 4. That one part in a million might mean all the difference.

Any wild hairs along this line will be nurtured tenderly by none other than Zar-Kan himself.

How's about it?

## METAMORPHOSIS, or HOW TO PERVERT A THEORY

By H. T. McAdams

It has been said, and truly, that the theories of one generation are perverted by the next. Such perversions are often enough to make great men turn over in their graves, and this fact offers little solace to contemporary scientists like Einstein and Heisenberg. The mundane purposed which relativity and uncertainty have already been made to serve are sufficient to insure that these men will indeed have a restless time when they have "shuffled off this mortal coil."

The metric process of going beyond the facts is known as extrapolation, and it is a method of the utmost utility to science fiction. Less familiar, perhaps, is the topological process, which, for want of a better term, may be called metamorphosis, a changing of form.

The prefix "meta-", from the Greek, means "beyond." Metaphysics, then, is literally "beyond physics", but it is a topological "beyond", rather than a metric "beyond." The subject-matter of metaphysics is non-empirical in nature, and to this extent at least, is topologically different from the "observables" of physics.

Elleston Trevor, in The Immortal Error (London, G. G. Swan), quoting an epigram of Hood, asks:

"What is mind? No matter. What is matter? Never mind. What is the soul? It is immaterial."

In other words, as any semanticist will agree, such questions are meaningless, because they are not capable of being answered by any meaningful operation. Yet Man, being the artist that he is, demands symmetry and continuity. To find them, he may need to devise a new discipline, a "meta-semantics" if you will, to take him literally "beyond meaning." Such a discipline might well be to epistemology what the philosophy of Ratsche was to ethics, for "beyond good and evil" lies something which we can classify only as "meta-ethics."

The logical positivists are concerned with "meta-languages", which are required in conjunction with the physical languages. When a statement is made in the "object language" concerning a space-time event, there must often be made, in turn, a statement about that statement, by way of the "meta-language." It is obvious that such an approach permits of infinite regression, forming a hierarchy of languages, each one of which is the subject matter for the one above.

Kurt Gödel, in attacking a similar problem in meta-mathematics, demonstrated that this snipe-hunt is more than an emotional frailty. Certain logical systems can not be proved consistent by their own methods of proof. Within a given system will be certain propositions whose validity can not be established by the rules of that system, though they can be seen to be true from a different point of view.

# LINEAR SPACES

By Don Bratton

Installment #1 of a series.

One of the recent conquests of mathematics is the notion of "linear space". It combines what is most essential in many fields of geometry, physics, theory of equations, etc. Like most mathematical ideas, once we have it, it is difficult to understand why the notion, being so simple, was not discovered earlier. With true simplicity comes an illusory feeling of "obviousness".

. The notion of linear space comes directly from the operation of addition of numbers. Addition is a process which obeys the following laws:

 $(A_7)$  a + (b + c) = (a + b) + c. ("Associative" law.)

(Ag) a+b = b+a ("Commutative" law.)

(A3) For each a, b, we can find a c such that

g+c=b (Existence of inverses.)

Note that Az takes into account the existence of negative numbers; for example, if a 2 10, b 24, then c = -6.

In many parts of algebra, the statements make use only of symbols like our a, b, c, in the above, and a "plus" sign. Mathematicians have found it convenient to use this fact to advantage. Such statements are organized around a system in which we pretend that we are dealing, not with numbers, but with general, or abstract "elements". We assume simply that our "elements" obey the three laws A1 2 3 and do not necessarily obey any particular others. This mental twist results in greater generality and simplicity of statement in mathematics. It has blossomed out into abstract algebra, a program which consistently carries out this new "method".

As examples of the wide range of applications of our "generalized addition", we give the following:

# 1. Displacements of Euclidean space.

Lat P be a point in space. Consider various displacements of this point. Label a displacement with a single letter. For example, a could stand for a displacement three inches upward, b a displacement



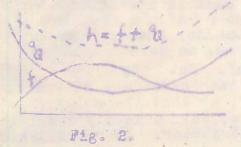
4 inches to the right, etc. We can define addition of these letters, or displacements. Let a, b be two displacements. Then "a + b" is defined as the total displacement resulting from first performing the displacement b, then performing the displacement a. (See figure 1.) It is readily seen that this "addition" of displacements obeys Al and Ag. How about Ag? Well, first note that for every displacement b, there is another which we might note as "-b" which is the opposite displacement, i. s. the dis-

placement of the same distance but in the opposite direction. It is convenient to consider "ne displacement at all" itself as a displacement, labeled "s", the "zero displacement". Then the displacements b, -b have the property that b + (-b) S z. Further, given two displacements a, b, we take c S b + (-a), (which is usually written for conventence simply "b - a"). Then a + b S b. Thus Az is satisfied.

It should be noted that when we write equations like "a + c 2 b"
we are not talking about the position or positions of the point P, but
about the interrelations of certain displacements of P. Thus we have
almost forgotten the original subject -- P -- and are interested
only in certain operations on it. ("Displacements" such as we have
been discussing are called "vectors" in physical literature. This is
perhaps due to an unwarranted tendency to make the abstract concrete.)

## 2. Addition of Functions

Consider functions, y = f(x), y = g(x), etc., x and y being real variables. Given two functions f, g, we can form a new function h, by addition: h(x) = f(x) + g(x). We then write "h a f + g" to show the relation between the functions. This affair is nicely pictured by a graph, which pictures a function as a curve. If f and g are plotted on a graph, then the curve representing h is found by adding the



heights of f and g at each point.

(See Figure 2). Addition of functions is seen to obey A1 and A2, and also A2. The reader might remark at this point, "Of course, we know immediately that this 'addition' of functions will obey all the rules of addition of numbers, because it consists simply of adding the numerical values of the functions." In this course of reasoning, the reader

would be dead wrong. To convince himself, he should try multiplying functions. In the latter case, the equation acc ab, in the given functions a, b, cannot always be solved for the unknown function c:

Les (f,g) be a pair of functions. When we say that "f equals g" (in symbols, "f = g"), we mean that f(x) = g(x) for all values of x. The "zero function" z is defined as the function z(x) = 0 for all values of x. It has the property that  $f \in z = f$  for all functions f. It is indeed the only function that has this property. If f is a function then there is another, written "-f", which is simply the function taking values numerically negative of those of f(x). It has the property that  $f \in (-f) = z$ . The equation f + h = g, in the given functions f, g, and the unknown function h, has the solution h = g + (-f), i. e., h = g - f.

Enough for our two examples. They are sufficient to show the variety of interpretations that can be put upon the laws A1 2 3. Being convinced of their power, we are let to talk about "additive groups", which by definition are simply any set of elements a, b, c, etc., together with an operation "+", which satisfies A1 2 3. The operation in any "additive group" can be written "+" without fear of confusion with numbers.

Let S be an additive group. The equation a be a, a being given, b an unknown, has a solution in b, since it is a special case of A3 Denote one solution by b1, so that b1 is a definite element and satisfies a b1 2 a. This element b1 has a deeper property than

we might have suspected. For let c be say given element. Then by A3. there exists a 2 such that c a a d. Then by c o bi fard) a (b) a) d a a d a c. Thus the element by is a solution for all such equations as c = a c. for various values of c! Such an element is called a "zero" element, and will hereafter be depoted 'z". We have demonstrated that there exists an element z satisfying a = z = a for all a.

boss an additive group have more than one spro! Does and a a have any other solution besides the solution of a by which we supposed found above! Wall, suppose a solution, so that a be a a Then by our previous reasoning, by is a sero element, i.e., of by a for all of the used only the property of by it the above that it was a solution of the equation; thus the conclusions reached apply to any solution.) In particular, this equation must seld for a bit has by a by But by was also a zero, so, conversely by to a but thus by a by by by the conclusions are answered.

Having demonstrated the swistence of negatives, we turn to the entirely general equation a + a = b, in the unknown a = 0. One solution is a = b + (-a), for

Purcher, this is the unions solution, for if a + eg o b, so that on it a solution [possibly the came] than, by adding -a to each member we have

(-a) f a + og o (-a) r b.

1.e. 3 + og 2 (-a) r b.

or og 2 b + (-a).

In an additive group an ampression like a + a + a can be obbreviated "3a". In general, if a is an integer positive, negative or zero, "na" can be appropriately defined. For a positive, "na" is defined as a + a + ... + a taken to a terms. For a = 0, "0a" is defined to be a for a negative "as" is defined to be a "multiplication" of the elaments of the group by integers, we see that

naja z (n + n)s. n(na) z (zm/a.

In order to discuss linear subspaces, it is necessary first to discuss the notion of "subgroup". Let S be an additive group, as was discussed above. Let T be a set made up of elements of S, but not necessarily containing all of the elements of S. (T is then said to be a "subset" of S.) If a, b are two elements in T, then, a fortion, a and a are in S, so a to denotes an element of S. Is a to also an element of S.

# THE TVE-FINGERED BEAST OF THAT INSUE #2 COVER

This was to be longer, but space does not permit. Whereas each of the distances among four points in 3-space (represented by the tetrahedron) can be varied independently of the others, the restriction imposed by the determinant does not allow this for five-points or more. Does this have anything to do with the fact that the human beaut svolved with five fingers and no more? And if so, what would be the most logical number of digits for a 4-dimensional or n-dimensional being?

LINEAR SPACES (concluded from p. 14)

for one thing. A subset T of an additive group S is said to be "closed" under the group operation when, for each s and b in T, a + b is also in T.

Example: In the set 3 of all displacements of a point F in Space, consider the subset T of those displacements all confined to a line -- that is, displacements to right and left, or upwards and downwards, for confined to any other direction. Such a subset T will be closed under the addition of displacements. Again, let T be all those displacements confined to a single plane, that is, up down right, and left, but not forward or backward, etc. Then again T is closed. In the set S of all functions f(x), consider the subset T of all polynomials. Since the sum of two polynomials is again a polynomial, T is closed. Likewise, the subset T of all continuous functions, or differentiable functions sto.

A subset T of an additive group S which is closed is called a subgroup of the original group.

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# METAMORPHOSIS (concluded from p. 11)

As a classic example of this logical anomaly, we may quote the paradox of Epimenides, the Cretan, who said that all Cretans are liars. It was in order to deviate the inevitable verbal repeating decimal of "true - false - true - false - true - false - true - ." that Bertrand Russell inaugurated his "theory of types" in which each statement is classified as to whether it is concerned with classes of things, classes of classes of things, classes of classes of things, classes of classes of things, and so on. Norzybski's "etsuctural differential" for representing different levels of abstraction is a similar approach. A "proof" at one level of the hierarchy does not necessarily imply a "croof" at a different level, because the two levels may be related in such a way that the one is substantially expost facto to the other. As Brouwer explains, "A implies the absurdity of the absurdity of A does not imply A."

In other words, to indulae in a bit of perversion surselves, it may be all right to pervert a theory, either by extrapolation or metamorphosis, so long as we do not justify that perversion by the wiels-sale superposition of the arguments which gave that theory birth. At is not A2, especially when they represent along and attitudes.

As the sailor said on shore laws, "It's not the same,"

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